## Chapter 4 The structure of diatomic molecules



1. Shroedinger equation of  $H_2^+$ 

#### **Born-Oppenheimer Approximation**

- The electrons are much lighter than the nuclei.
- Nuclear motion is slow relative to the electron motion.

#### The hamiltonian operator

$$\hat{H} = -\frac{1}{2}\nabla_e^2 - \frac{1}{r_a} - \frac{1}{r_b} + \frac{1}{R}$$
Shroedinger equation of H<sub>2</sub><sup>+</sup>

$$\hat{H}\psi = E\psi$$



Where  $r_a$  and  $r_b$  are related by:

$$r_b = \sqrt{r_a^2 + R^2 - 2r_a R \cos\theta}$$

#### Molecular Orbital Theory

### $H_2^+$

We could now solve:  $\hat{H}(r_1, R)\psi(r_1, R) = E_e(R)\psi(r_1, R)$ 

This is possible but tedious

 $H_2^+$  can be solved exactly using confocal elliptical coordinates:



 $\begin{aligned} \xi &= (r_a + r_b)/R \\ \eta &= (r_a - r_b)/R \\ \phi \text{ is a rotation around } z \end{aligned}$ 

 $0 \le \phi \le 2\pi;$   $1 \le \xi \le \infty;$  $-1 \le \eta \le 1$   $\overline{\psi_{elec}} = F(\xi,\eta) (2\pi)^{-1/2} e^{im\phi}$ where m=0, ±1, ±2, ±3,

The associated quantum number is  $\lambda$ .  $\rightarrow$  orbital angular momentum  $\lambda = |m|$ 

Each electronic level with  $m \neq 0$  is doubly degenerate, i.e. + |m|,-|m|

atoms:  $\ell = 0, 1, 2, ...$  and the atomic orbitals are called: s,p,d, etc.

diatomics:  $\lambda = 0, 1, 2, ...$  and the molecular orbitals are:  $\sigma$ ,  $\pi$ ,  $\delta$ , etc.

λ	0	1	2	3	4
letter	σ	π	δ	φ	γ

 $\psi_{\text{elec}} = F(\xi, \eta) \ (2\pi)^{-1/2} \ e^{im\phi}$ 



#### 2. The Variation Theorem

For any well-behaved wavefunction  $\phi$ , the average energy from the Hamiltonian of the system is always greater or close to the exact ground state energy (E<sub>0</sub>) for that Hamiltonian,

 $<\!E\!>=\!\frac{\int \phi^* \hat{H} \phi d\tau}{\int \phi^* \phi d\tau} \ge E_0$ 

**Example:** Devise a trial variation function for the particle in a one-dimensional box of length l.

A simple function that has the properties of the ground state is the parabolic function:

 $\phi = x(l-x)$ 

0

$$\int \phi^* \hat{H} \phi d\tau = -\frac{\hbar^2}{2m} \int_0^l (lx - x^2) \frac{d^2}{dx^2} (lx - x^2) dx = \frac{\hbar^2 l^2}{6m}$$

for  $0 \le x \le l$ 

$$\int \phi^* \phi d\tau = \int_0^l x^2 (l-x)^2 dx = \frac{l^5}{30}$$

$$<\!E\!>=\!\frac{\int \phi^* \hat{H} \phi d\tau}{\int \phi^* \phi d\tau} =\!\frac{5h^2}{4\pi^2 ml^2} \ge\!\frac{h^2}{8ml^2}$$

Proof  

$$\phi(\varepsilon \ge E_{0}) \text{ its } ground \text{ state } (\psi_{0} \to E_{0})$$

$$\phi = \sum_{i} c_{i}\psi_{i}$$

$$\hat{H}\psi_{i} = E_{i}\psi_{i}$$

$$E_{i} \ge E_{0}$$

$$< E \ge \frac{\int \phi^{*}\hat{H}\phi d\tau}{\int \phi^{*}\phi d\tau}$$
The Eigenfunctions of an Hermitian operator consist of a complete set.  $\psi_{1}, \psi_{2}, \psi_{3} \dots \text{ consist of an orthogonal normalized set of wavefunctions}$ 

$$\int \phi^{*}\phi d\tau = \int \sum_{i} c_{i}^{*}\psi_{i}^{*}\sum_{j} c_{j}\psi_{j}d\tau = \sum_{i} c_{i}^{*}\sum_{j} c_{j}\int \psi_{i}^{*}\psi_{j}d\tau$$

$$= \sum_{i} \sum_{j} c_{i}c_{j}\delta_{ij} = \sum_{i} |c_{i}|^{2}$$

$$\int \phi^{*}\hat{H}\phi d\tau = \int \sum_{i} c_{i}^{*}\psi_{i}^{*}\hat{H}\sum_{j} c_{j}\psi_{j}d\tau = \sum_{i} c_{i}^{*}\sum_{j} c_{j}\int \psi_{i}^{*}\hat{H}\psi_{j}d\tau$$

$$= \sum_{i} \sum_{j} c_{i}c_{j}\int \psi_{i}^{*}E_{j}\psi_{j}d\tau = \sum_{i} \sum_{j} c_{i}c_{j}E_{j}\int \psi_{i}^{*}\psi_{j}d\tau = \sum_{i} |c_{i}|^{2}E_{j}$$

$$\varepsilon = \langle E \ge \frac{\sum_{i} |c_{i}|^{2}E_{j}}{\sum_{i} |c_{i}|^{2}} \ge E_{0}$$

#### 3. Linear Variation Functions

$$\phi = c_1 f_1 + c_2 f_2 + \dots + c_n f_n = \sum_{j=1}^n c_j f_j$$

A linear variation function is a linear combination of n linearly independent functions  $f_1, f_2, ..., f_n$ .

Based on this principle, the parameters are regulated by the minimization routine so as to obtain the wavefunction that corresponds to the minimum energy. This is taken to be the wavefunction that closely approximates the ground state.

$$<\!E\!\!>=\!\!\frac{\int \phi^* \hat{H} \phi d\tau}{\int \phi^* \phi d\tau} \ge E_0$$
$$\mathcal{E} =<\!\!E\!>$$

adjusting the parameter, make 
$$\frac{\partial \varepsilon}{\partial c_i} = 0$$

Example  

$$\phi = c_1 \psi_1 + c_2 \psi_2 \qquad \varepsilon = \frac{\int \phi^* \hat{H} \phi d\tau}{\int \phi^* \phi d\tau}$$

$$\int \phi^* \phi d\tau = \int (c_1 \psi_1 + c_2 \psi_2)^* (c_1 \psi_1 + c_2 \psi_2) d\tau$$

$$= \int (c_1^2 \psi_1^* \psi_1 + c_1 c_2 \psi_1^* \psi_2 + c_1 c_2 \psi_2^* \psi_1 + c_2^2 \psi_2^* \psi_2) d\tau$$

$$= \int (c_1^2 \psi_1^* \psi_1 + 2c_1 c_2 \psi_1^* \psi_2 + c_2^2 \psi_2^* \psi_2) d\tau$$

$$= c_1^2 + 2c_1 c_2 S_{12} + c_2^2 \qquad (S_{ij} = \int \psi_1^* \psi_j d\tau = S_{ji})$$

$$= c_1^2 S_{11} + 2c_1 c_2 S_{12} + c_2^2 S_{22} \qquad (S_{11} = S_{22} = 1)$$

$$\int \phi^{*} \hat{H} \phi d\tau = \int (c_{1}\psi_{1} + c_{2}\psi_{2})^{*} \hat{H}(c_{1}\psi_{1} + c_{2}\psi_{2}) d\tau$$
  
= 
$$\int (c_{1}^{2}\psi_{1}^{*} \hat{H}\psi_{1} + c_{1}c_{2}\psi_{1}^{*} \hat{H}\psi_{2} + c_{1}c_{2}\psi_{2}^{*} \hat{H}\psi_{1} + c_{2}^{2}\psi_{2}^{*} \hat{H}\psi_{2}) d\tau$$
  
= 
$$c_{1}^{2}H_{11} + 2c_{1}c_{2}H_{12} + c_{2}^{2}H_{22} \qquad (H_{ij} = H_{ji} = \int \psi_{i}^{*} \hat{H}\psi_{j}) (H_{11} = H_{22} = 1)$$

$$let \qquad \varepsilon = \frac{c_1^{-2}H_{11} + 2c_1c_2H_{12} + c_2^{-2}H_{22}}{c_1^{-2}S_{11} + 2c_1c_2S_{12} + c_2^{-2}S_{22}} = \frac{y}{x}$$

$$make \qquad \varepsilon \Rightarrow E_0$$

$$0 = \frac{\partial\varepsilon}{\partial c_1} = \frac{1}{x}\frac{\partial y}{\partial c_1} - \frac{y}{x^2}\frac{\partial x}{\partial c_1}$$

$$= \frac{1}{x}(2c_1H_{11} + 2c_2H_{12}) - \frac{y}{x^2}(2c_1S_{11} + 2c_2S_{12})$$

$$(2c_1H_{11} + 2c_2H_{12}) - \frac{c_1^{-2}H_{11} + 2c_1c_2H_{12} + c_2^{-2}H_{22}}{c_1^{-2}S_{12} + c_2^{-2}S_{22}}(2c_1S_{11} + 2c_2S_{12}) = 0$$

$$(2c_1H_{11} + 2c_2H_{12}) - E(2c_1S_{11} + 2c_2S_{12}) = 0$$

$$(c_1H_{11} + c_2H_{12}) - E(c_1S_{11} + c_2S_{12}) = 0$$

$$(H_{11} - ES_{11})c_1 + (H_{12} - ES_{12})c_2 = 0$$

$$(1)$$
same as
$$0 = \frac{\partial\varepsilon}{\partial c_2}$$

$$(H_{21} - ES_{21})c_1 + (H_{22} - ES_{22})c_2 = 0$$

$$(2)$$

seqular equation made equation resolved $(c_1, c_2 \neq 0)$   $\begin{vmatrix} H_{11} - ES_{11} & H_{12} - ES_{12} \\ H_{21} - ES_{21} & H_{22} - ES_{22} \end{vmatrix} = 0$ get  $E \Rightarrow$  get  $c_1, c_2 \Rightarrow$  get  $\phi$ The algebraic equation has 2 roots,  $E_1$  and  $E_2$ .  $\phi = c_1\psi_1 + c_2\psi_2 + ... + c_n\psi_n$  $\begin{vmatrix} H_{11} - ES_{11} & H_{12} - ES_{12} & ... & H_{1n} - ES_{1n} \\ H_{21} - ES_{21} & H_{22} - ES_{22} & ... & H_{2n} - ES_{2n} \\ . & . & ... & ... \\ H_{n1} - ES_{n1} & H_{n2} - ES_{n2} & ... & H_{nn} - ES_{nn} \end{vmatrix} = 0$ 

The algebraic equation has *n* roots, which can be shown to be real. Arranging these roots in order of increasing value:  $E_1 \le E_2 \le ... \le E_n$ .

• From the variation theorem, we know that the lowest value of root  $(W_1)$  is the upper bound for the system's ground-state energy.

 $E_1 \leq W_1$ 

•Moreover, it can be proved that the linear variation method provides upper bounds to the energies of the lowest n states of the system.

 $E_2 \le W_{2,} E_3 \le W_{3,} \dots, E_n \le W_{n,}$ 

• We use the roots as approximations to the energies of the lowest states.

• If approximation to the energies of more states are wanted, we add more functions  $f_k$  to the trial function  $\phi$ .

• The addition of more functions  $f_k$  can be shown to increase the accuracy of the previously calculated energies.



$$\phi = c_a \psi_a + c_b \psi_b$$
seqular equation
$$\left|\begin{array}{c}H_{aa} - ES_{aa} & H_{ab} - ES_{ab}\\H_{ba} - ES_{ba} & H_{bb} - ES_{bb}\end{array}\right| = 0$$

$$\because \psi_a \text{ has the same form as }\psi_b \qquad \therefore H_{aa} = H_{bb}, \qquad H_{ab} = H_{ba}$$

$$\left(H_{aa} - ES_{aa}\right)^2 = \left(H_{ab} - ES_{ab}\right)^2$$

$$H_{aa} - ES_{aa} = \pm \left(H_{ab} - ES_{ab}\right)$$
if 
$$H_{aa} - ES_{aa} = -\left(H_{ab} - ES_{ab}\right)$$

$$E_1 = \frac{H_{aa} + H_{ab}}{1 + S_{ab}} = \frac{\alpha + \beta}{1 + S}$$
if 
$$H_{aa} - ES_{aa} = H_{ab} - ES_{ab}$$

$$E_2 = \frac{H_{aa} - H_{ab}}{1 - S_{ab}} = \frac{\alpha - \beta}{1 - S}$$

substituting	$E_1$	to	seqular	equation
$(H_{aa} - ES_{aa})c_a$	$+(H_{ab}$	$-ES_{ab}$	$c_{b} = 0$	(1)
$(H_{ba} - ES_{ba})c_a$	$+(H_{bb}$	$-ES_{bb}$	$c_b = 0$	(2)

$$\begin{split} S_{aa} &= S_{bb} = 1 \\ (H_{aa} - \frac{H_{aa} + H_{ab}}{1 + S_{ab}})c_a + (H_{ab} - \frac{H_{aa} + H_{ab}}{1 + S_{ab}}S_{ab})c_b = 0 \\ (H_{aa}(1 + S_{ab}) - (H_{aa} + H_{ab}))c_a + (H_{ab}(1 + S_{ab}) - (H_{aa} + H_{ab})S_{ab})c_b = 0 \\ (H_{aa}(1 + S_{ab}) - (H_{aa} + H_{ab}))c_a + (H_{ab}(1 + S_{ab}) - (H_{aa} + H_{ab})S_{ab})c_b = 0 \\ (H_{aa}S_{ab} - H_{ab})c_a + (H_{ab} - H_{aa}S_{ab})c_b = 0 \\ (H_{aa}S_{ab} - H_{ab})c_a + (H_{ab} - H_{aa}S_{ab})c_b = 0 \\ c_a - c_b = 0 \qquad c_a = c_b \\ \phi_1 = c_a\psi_a + c_b\psi_b = c_a(\psi_a + \psi_b) \end{split}$$

nomalization condition 
$$\int \phi_1^* \phi_1 = 1$$
$$\int (c_a(\psi_a + \psi_b))^* c_a(\psi_a + \psi_b) d\tau = 1$$
$$\int [c_a^2 \psi_a^2 + 2c_a^2 \psi_a \psi_b + c_a^2 \psi_b^2] d\tau = 1$$
$$2c_a^2 (1 + S_{ab}) = 1$$
$$\therefore \quad c_a = \frac{1}{\sqrt{2(1 + S_{ab})}}$$
$$\phi_1 = \frac{1}{\sqrt{2(1 + S_{ab})}} (\psi_a + \psi_b)$$
substituting  $E_2$  to seqular equation  $c_a + c_b = 0$   $c_a = -c_b$   
 $\phi_2 = c_a \psi_a + c_b \psi_b = c_a (\psi_a - \psi_b)$ 
$$\phi_2 = \frac{1}{\sqrt{2(1 - S_{ab})}} (\psi_a - \psi_b)$$



Overlap  
integral
$$S_{ab} = \int \psi_a^* \psi_b d\tau$$

$$H_{aa} = \int \psi_a^* \hat{H} \psi_a d\tau$$

$$\hat{H} = -\frac{1}{2} \nabla^2 - \frac{1}{r_a} - \frac{1}{r_b} + \frac{1}{R}$$

$$H_{aa} = \int \psi_a^* (-\frac{1}{2} \nabla^2 - \frac{1}{r_a} - \frac{1}{r_b} + \frac{1}{R}) \psi_a d\tau$$

$$= \int \psi_a^* (-\frac{1}{2} \nabla^2 - \frac{1}{r_a}) \psi_a d\tau + \int \psi_a^* \frac{1}{R} \psi_a d\tau - \int \psi_a^* \frac{1}{r_b} \psi_a d\tau$$

$$= E_H + \frac{1}{R} - \int \psi_a^* \frac{1}{r_b} \psi_a d\tau = E_H + J$$

$$J \approx 5.5\% E_H$$

$$\therefore \qquad H_{aa} = E_H + J \approx E_a = \alpha$$

## resonance integral

$$\begin{split} H_{ab} &= \int \psi_a^* \hat{H} \psi_b d\tau \\ H_{ab} &= \int \psi_a^* (-\frac{1}{2} \nabla^2 - \frac{1}{r_a} - \frac{1}{r_b} + \frac{1}{R}) \psi_b d\tau \\ &= \int \psi_a^* (-\frac{1}{2} \nabla^2 - \frac{1}{r_b}) \psi_b d\tau + \int \psi_a^* (-\frac{1}{r_a} + \frac{1}{R}) \psi_b d\tau \\ &= \int \psi_a^* E_b \psi_b d\tau + \frac{1}{R} \int \psi_a^* \psi_b d\tau - \int \psi_a^* \frac{1}{r_a} \psi_b d\tau \\ &= E_H S_{ab} + \frac{S_{ab}}{R} - \int \psi_a^* \frac{1}{r_a} \psi_b d\tau \\ &= E_H S_{ab} + K \\ &= \beta \end{split}$$

$$\begin{split} S_{ab} &= \int \psi_a^* \psi_b d\tau = S \\ H_{aa} &= E_H + J \approx E_a = \alpha \\ H_{ab} &= E_H S_{ab} + K = \beta \\ E_a &= \frac{H_{aa} + H_{ab}}{1 + S_{ab}} \\ E_b &= \frac{H_{aa} - H_{ab}}{1 - S_{ab}} \\ E_1 &= \frac{E_H + J + E_H S_{ab} + K}{1 + S_{ab}} = E_H + \frac{J + K}{1 + S} \\ E_2 &= E_H + \frac{J - K}{1 - S} \end{split}$$

# **H**<sup>+</sup>2





# **H**<sup>+</sup><sub>2</sub>

A representation of the constructive interference that occurs when two H 1s orbitals overlap and form a bonding  $\sigma$  orbital.

$$\phi_1 = \frac{1}{\sqrt{2(1+S_{ab})}} (\psi_a + \psi_b)$$

### Molecular Orbital Theory

# **H**<sup>+</sup><sub>2</sub>



The electron density calculated by forming the square of the wavefunction. Note the accumulation of electron density in the internuclear region.

$$\rho(1) = \frac{1}{2(1+S)} \psi_a^2 + \frac{1}{2(1+S)} \psi_b^2 + 2\frac{1}{2(1+S)} \psi_a \psi_b$$

 $\sigma_{s}^{*}$ 

# **H**<sup>+</sup><sub>2</sub>

A representation of the destructive interference that occurs when two H1s orbitals overlap and form an antibonding  $\sigma^*$  orbital.

$$\phi_2 = \frac{1}{\sqrt{2(1 - S_{ab})}} (\psi_a - \psi_b)$$

#### Molecular Orbital Theory





The electron density calculated by forming the square of the Wavefunction. Note the elimination of electron density from the internuclear region.

$$\rho(1) = \frac{1}{2(1-S)} \psi_a^2 + \frac{1}{2(1-S)} \psi_b^2 - 2\frac{1}{2(1-S)} \psi_a \psi_b$$



## $H_2^+$

A molecular orbital energy level diagram for orbitals constructed from the overlap of H1s orbitals; the separation of the levels corresponds to that found at the equilibrium bond length.

#### § 2 Molecular orbital theory and diatomic molecules

1. Molecular orbital theory

a. Every electron in a molecule is in an average potential field of the nuclei and the other electrons.

The state of electron i is described by the  $\psi_i$  wavefunction.

--- the one-electron wavefunction

$$\varphi(1,2,...n) = \psi_1(1)\psi_2(2)...\psi_n(n)$$
$$\hat{H} = \sum_i \hat{H}_i$$
$$\hat{H}_i\psi_i = E_i\psi_i$$

#### b. The formation of molecular orbital (MO).

The MO may be approximated from the linear combination of atomic orbitals (LCAO).

Three basic requirements in the formation of MO:

The AOs should

- \* have comparable energy,
- \* have compatible symmetry,
- \* be able to have maximum overlap.





### Why should the AOs should have comparable energy?

$$\begin{split} \phi &= c_a \psi_a + c_b \psi_b \\ seqular & equation \\ \left| \begin{array}{c} H_{aa} - ES_{aa} & H_{ab} - ES_{ab} \\ H_{ba} - ES_{ba} & H_{bb} - ES_{bb} \end{array} \right| = 0 \\ \text{if } H_{aa} &= E_a, H_{bb} = E_b, H_{ab} = \beta, S_{ab} = 0 \\ E_1 &= \frac{1}{2} [(E_a + E_b) - \sqrt{(E_b - E_a)^2 + 4\beta^2}] \\ E_2 &= \frac{1}{2} [(E_a + E_b) + \sqrt{(E_b - E_a)^2 + 4\beta^2}] \\ \end{bmatrix}$$

$$\begin{aligned} & \begin{array}{c} E_a \\ E_a \\ E_b \end{array} \\ \hline \\ E_1 \\ \hline \\ E_1 \\ \hline \\ E_1 \\ \hline \\ \end{array} \\ \end{aligned}$$

$$\begin{aligned} & \begin{array}{c} (E_b - E_a) >> |\beta| \\ E_b = E_a \\ \hline \\ E_b = E_a \end{array} \\ \hline \\ \end{array} \\ \end{aligned}$$

#### b. The formation of molecular orbital (MO).

The MO may be approximated from the linear combination of atomic orbitals (LCAO).

Three basic requirements in the formation of MO:

\* The AOs should have comparable energy, have compatible symmetry and be able to have maximum overlap.

The building-up principle in molecules:

Pauli exclusion principle, the minimum energy priciple and Hund's rule.

2. The characteristic distribution and classification of molecular orbital

### a. $\sigma$ -orbital and $\sigma$ -bond







2. The characteristic distribution and classification of molecular orbital

### b. $\pi$ -orbital and $\pi$ -bond



2. The characteristic distribution and classification of molecular orbital

c.  $\delta$ -orbital and  $\delta$ -bond



- 3. The structure of homonuclear diatomic molecules
- a. The ground state electronic configurations



#### Molecular Orbital Theory



The effect of interactions between 2s and 2p.

At the start of the second row Li-N, we have mixing of 2s and 2p. The result is that  $1\sigma_u^*$  is pushed down in energy whereas  $2\sigma_g$  is raised.

**B<sub>2</sub>:** KK $(1\sigma_g)^2 (1\sigma_u)^2 (1\pi_u)^2$ 

N<sub>2</sub>: KK $(1\sigma_g)^2 (1\sigma_u)^2 (1\pi_u)^4 (2\sigma_g)^2$ 



H <sub>2</sub>	2	$(\sigma_{g1S})^2$
$\mathrm{He_2}^+$	3	$(\sigma_{g1s})^2 (\sigma_{u1s})^1$
Li <sub>2</sub>	6	$\mathrm{KK}(1\sigma_{\mathrm{g}})^{2}$
B <sub>2</sub>	10	$\mathrm{KK}(1\sigma_{\mathrm{g}})^{2}(1\sigma_{\mathrm{u}})^{2}(1\pi_{\mathrm{u}})^{2}$
C <sub>2</sub>	12	$\mathrm{KK}(1\sigma_{\mathrm{g}})^{2}(1\sigma_{\mathrm{u}})^{2}(1\pi_{\mathrm{u}})^{4}$
$N_2^+$	13	$\mathrm{KK}(1\sigma_{\mathrm{g}})^{2}(1\sigma_{\mathrm{u}})^{2}(1\pi_{\mathrm{u}})^{4}(2\sigma_{\mathrm{g}})^{1}$
N <sub>2</sub>	14	$\mathrm{KK}(1\sigma_{\mathrm{g}})^{2}(1\sigma_{\mathrm{u}})^{2}(1\pi_{\mathrm{u}})^{4}(2\sigma_{\mathrm{g}})^{2}$
$O_2^+$	15	$KK(\sigma_{g2s})^{2}(\sigma_{u2s})^{2}(\sigma_{g2p})^{2}(\pi_{u2p})^{4}(\pi_{g2p})^{1}$
O <sub>2</sub>	16	$\mathrm{KK}(\sigma_{\mathrm{g2s}})^{2} \left(\sigma_{\mathrm{u2s}}\right)^{2} \left(\sigma_{\mathrm{g2p}}\right)^{2} \left(\pi_{\mathrm{u2p}}\right)^{4} \left(\pi_{\mathrm{g2p}}\right)^{2}$
F <sub>2</sub>	18	$KK(\sigma_{g2s})^{2}(\sigma_{u2s})^{2}(\sigma_{g2p})^{2}(\pi_{u2p})^{4}(\pi_{g2p})^{4}$

- 3. The structure of homonuclear diatomic molecules
- b. The bond order

Bond orders : b =  $\frac{1}{2}(n - n^{*})$ 

> n: Electrons in bonding orbitals n\*:Electrons in antibonding orbitals













### MO Theory for Heteronuclear Diatomics

- MO's will no longer contain equal contributions from each AO.
  - AO's interact if symmetries are compatible.
  - AO's interact if energies are close.
  - No interaction will occur if energies are too far apart. A nonbonding orbital will form.





 $\Psi_{\gamma}$  makes a greater contribution to the  $\Psi_{MO}$ 

## **Example: HF**

- The F (2s) is much lower in energy than the H (1s) so they do not mix.
  - The F (2s) orbital makes a non-bonding MO.
  - We certainly don't have to worry about the F (1s) because is MUCH lower in energy.
- The H (1s) and F (2p)'s are close in energy and do interact.
  - The 2px and 2py don't have the appropriate symmetry though and therefore form nonbonding MO'S
  - Only the 2pz and 1s mix.



#### K(2 σ)<sup>2</sup> (3 σ)<sup>2</sup> (1 π)<sup>4</sup>

#### **Isoelectronic rule:**

The MO's bond formation and electronic configurations are similar among the isoelectronic diatomic molecules.

### CO is isoelectronic with N<sub>2</sub>.

KK(3 σ)<sup>2</sup> (4 σ)<sup>2</sup> (1 π)<sup>4</sup> (5 σ)<sup>2</sup>



electronic configurations of NO

Molecule	electrons	electronic configuration	term
LiH	4	K(2 σ ) <sup>2</sup>	1 \Sec +
BeH	5	K(2 σ ) <sup>2</sup> (3 σ ) <sup>1</sup>	2 <u>&gt;</u> +
СН	7	K(2 σ) <sup>2</sup> (3 σ) <sup>2</sup> (1 π) <sup>1</sup>	<sup>2</sup> ∏
NH	8	K(2 σ) <sup>2</sup> (3 σ) <sup>2</sup> (1 π) <sup>2</sup>	3 <u>&gt;</u>
ОН	9	K(2 σ ) <sup>2</sup> (3 σ ) <sup>2</sup> (1 π ) <sup>3</sup>	<sup>2</sup> ∏
HF	10	K(2 σ) <sup>2</sup> (3 σ) <sup>2</sup> (1 π) <sup>4</sup>	1 <u>&gt;</u> +
BeO , BN	12	KK $(3 \sigma)^2 (4 \sigma)^2 (1 \pi)^4$	1 \Sec +
CN , BeF	13	KK $(3 \sigma)^2 (4 \sigma)^2 (1 \pi)^4 (5 \sigma)^1$	2 <u>&gt;</u> +
CO	14	KK $(3 \sigma)^2 (4 \sigma)^2 (1 \pi)^4 (5 \sigma)^2$	1 \Sec +
NO	15	KK $(3 \sigma)^2 (4 \sigma)^2 (1 \pi)^4 (5 \sigma)^2 (2 \pi)^1$	2∏







## Comparison of MO and VB theories

#### **VB** Theory

- Separate atoms are brought together to form molecules.
- The electrons in the molecule *pair* to accumulate density in the internuclear region.
- The accumulated electron density "holds" the molecule together.
- Electrons are *localized* (belong to specific bonds).
- Hybridization of atomic orbitals
- Basis of Lewis structures, resonance, and hybridization.
- Good theory for predicting molecular structure.

#### **Molecular orbital theory**

- Molecular orbitals are formed by the overlap and interaction of atomic orbitals.
- Electrons then fill the molecular orbitals according to the aufbau principle.
- Electrons are *delocalized* (don't belong to particular bonds, but are spread throughout the molecule).
- Can give accurate bond dissociation energies if the model combines enough atomic orbitals to form molecular orbitals.